SI Session: Sept. 8^{th} , 10^{th} & 12^{th} , 2008 Prof. Stockton : Calculus III

Mondays: 1:30 PM – 3:00 PM Fall 2008

Wednesdays: 4:50 PM – 6:20 PM SI Leader : Neil Jody Fridays: 1:00 PM – 2:30 PM

Room 1239 SNAD

[1] Let
$$\vec{u} = 2\hat{i} + \hat{j} - 2\vec{k}$$
 and $\vec{v} = -\hat{j} + 3\hat{k}$.

(a) Find the vector which has the same length as \vec{u} and the opposite direction as \vec{v} .

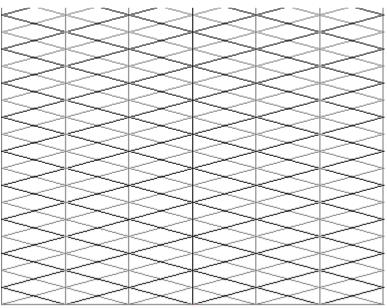
(b) Determine if the vector $\vec{w} = 6\hat{i} + \hat{j}$ lies in the plane of \vec{u} and \vec{v} .

(c) Find all unit vectors which are orthogonal to both \vec{u} and \vec{v} .

(d) Find the angle between \vec{u} and \vec{v} .

[2] Find the vector that has length 3 and has the opposite direction as $\langle -1,2,4 \rangle$.

[3] Let $\vec{u} = \langle -1,4,-2 \rangle$. Find a vector \vec{v} such that the area of the parallelogram spanned by \vec{u} and \vec{v} is 10.



- [4] Find a set of parametric equations of the described line.
- (a) The line that passes through the point (-4,5,2) and is parallel to the *xy*-plane and the *yz*-plane.

(b) The line that passes through the point (-4,5,2) and is perpendicular to the plane given by -x + 2y + z = 5.

(c) The line that passes through the point (-1,4,-3) and is parallel to $\vec{v} = 5\hat{i} - \hat{j}$.

(d) The line that passes through the point (-6,0,8) and is parallel to the line x=5-2t, y=2t-4, z=0.

- [5] Find an equation of the described plane.
- (a) The plane that passes through (2,3,-2), (3,4,2), and (1,-1,0).

(b) The plane that passes through the point (1,2,3) and parallel to the yz-plane.

(c) The plane that passes through the points (3,2,1) and (3,1,-5) and is perpendicular to the plane 6x + 7y + 2z = 10.

(d) The plane that passes through the points (4,2,1) and (-3,5,7) and is parallel to the *z*-axis.

[6] Determine all values of c such that the angle between the vectors $\vec{u} = \langle -1,0,1 \rangle$ and $\vec{v} = \langle c,3,1 \rangle$ is 45°.

[7] Find parametric equations for the line through (3, 1, -2) that intersects and is perpendicular to the line given by: x = -1 + t, y = -2 + t, z = -1 + t.

[8] Find an equation of the plane that contains the following lines:

$$l_1: x = t, y = 2 - t, z = 2 + 3t$$
 and $l_2: x = 1 + 4t, y = 1, z = 5 + 2t$

[9] Find the distance from the point (1,2,3) to the plane x + y - 2z = 1.