

SI Session: Oct. 20<sup>th</sup> & 22<sup>nd</sup>, 2008  
Mondays: 1:30 PM – 3:00 PM & 4:50  
PM – 6:20 PM  
Wednesdays: 1:30 PM – 3:00 PM &  
4:50 PM – 6:20 PM  
Room 1239 SNAD(Wed. early rm. 1121)

Prof. Stockton : Calculus III  
Fall 2008  
SI Leader : Neil Jody

[1] Find the directional derivative of the function at  $P$  in the direction of  $\vec{v}$ .

(a)  $g(x, y) = \arccos xy, P(1, 0), \vec{v} = \hat{i} + 5\hat{j}$

(b)  $h(x, y) = e^{-(x^2+y^2)}, P(0, 0), \vec{v} = \hat{i} + \hat{j}$

(c)  $h(x, y, z) = xyz, P(2, 1, 1), \vec{v} = \langle 2, 1, 2 \rangle$

[2] Find the directional derivative of the function at  $P$  in the direction of  $Q$ .

(a)  $f(x, y) = \cos(x + y), P(0, \pi), Q\left(\frac{\pi}{2}, 0\right)$

(b)  $g(x, y, z) = xye^z, P(2, 4, 0), Q(0, 0, 0)$

[3] Find the direction of maximum increase of the function at the given point.

(a)  $g(x, y) = ye^{-x^2}, (0, 5)$

(b)  $w = xy^2z^2, (2, 1, 1)$

- [4] The surface of a mountain is modeled by the equation  $h(x, y) = 5000 - 0.001x^2 - 0.004y^2$ . A mountain climber is at the point  $(500, 300, 4390)$ . In what direction should the climber move in order to ascend at the greatest rate?

- [5] A ground-dwelling cold hairy spider wants to get warm. The temperature at the point  $(x, y)$  is given by  $T(x, y) = x^2 - xy + 2y^2$  (degrees Fahrenheit). If the spider is at the point  $(2, 3)$ , in which direction should it move to increase its temperature the fastest?

- [6] At time  $t = 0$  (seconds), a particle is ejected from the surface  $x^2 + y^2 - z^2 = -1$  at the point  $(1, 1, \sqrt{3})$  in a direction normal to the surface at a speed of 10 units per second. When and where does the particle cross the  $xy$ -plane?

[7] Find an equation of the tangent plane at the given point.

(a)  $z = x^2 - 2xy + y^2, (1, 2, 1)$

(b)  $x = y(2z - 3), (4, 4, 2)$

[8] Find an equation of the plane tangent to the surface  $xyz - 4xz^3 + y^3 = 10$  at the point  $(-1, 2, 1)$ . Then find the angle between this tangent plane and the  $xy$ -plane.

[9] Find the directional derivative of the function  $f(x, y, z) = 3xz - 2xy^2$  at the point  $(-1, 1, 2)$  in the direction from  $(-1, 1, 2)$  to  $(1, 3, 3)$ .

[10] Let  $f(x, y) = \sqrt{x^2 + y}$ . Find an equation of the plane tangent to the graph of  $f$  at the point  $(-1, 3, 2)$ .

[11] Find an equation of the tangent plane to the surface at the given point.

(a)  $z = \arctan\left(\frac{y}{x}\right), \left(1, 1, \frac{\pi}{4}\right)$

[13] Find the gradient and the direction of maximum decrease at the given point.

(a)  $z = e^{-x} \cos y, \left(0, \frac{\pi}{4}\right)$

(b)  $z = \frac{x^2}{x-y}, (2,1)$

[14] Find an equation of the tangent plane and parametric equations of the line normal to the surface at the given point.

(a)  $z = -9 + 4x - 6y - x^2 - y^2, (2, -3, 4)$

(b)  $z = \sqrt{9 - x^2 - y^2}$ ,  $(1, 2, 2)$

[15] Find the critical points of the following functions.

(a)  $f(x, y) = x^3 - 3xy + y^2$

(b)  $f(x, y) = 2x^2 + 6xy + 9y^2 + 8x + 14$



$$(c) f(x, y) = xy + \frac{1}{x} + \frac{1}{y}$$