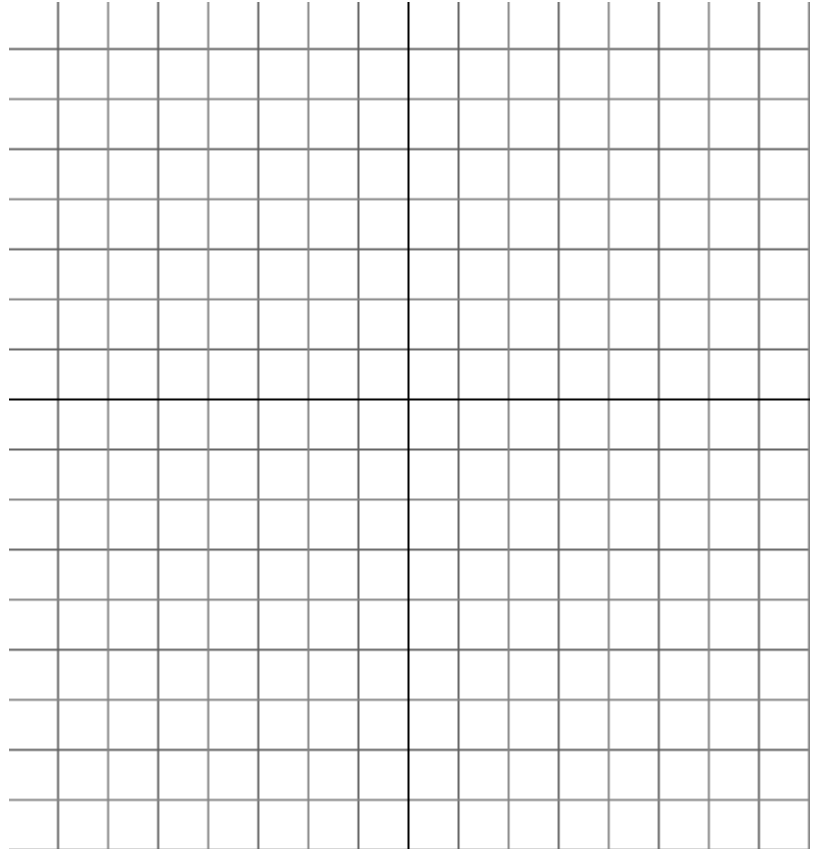
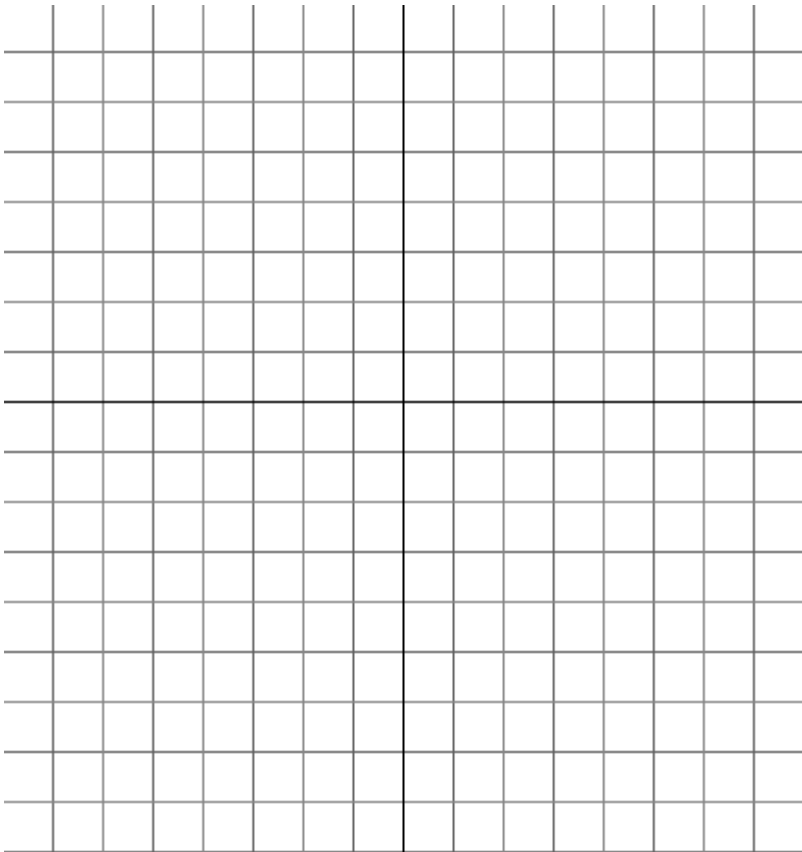


- [1] Let R denote the region in the xy -plane bounded by the graphs of $y = \ln x$, $y = 1$, and $y = 1 - x$. For each of the following, write down an integral representing the volume of the solid obtained by revolving R about the indicated line:
- (a) the x -axis (b) the y -axis (c) the line $x = -2$
(d) the line $y = 2$ (e) the line $x = 4$ (f) the line $y = -1$



[2] Let C be the portion of the graph of $y = \cos x + 2$ corresponding to $\frac{\pi}{2} \leq x \leq \pi$. Write down an integral representing each of the following:

- (a) the length of C
- (b) the area of the surface obtained by revolving C about the x -axis
- (c) the area of the surface obtained by revolving C about the y -axis
- (d) the area of the surface obtained by revolving C about the line $x = 4$
- (e) the area of the surface obtained by revolving C about the line $y = 3$
- (f) the area of the surface obtained by revolving C about the line $x = -2$
- (g) the area of the surface obtained by revolving C about the line $y = -1$



[3] Find the (arc) length of each curve.

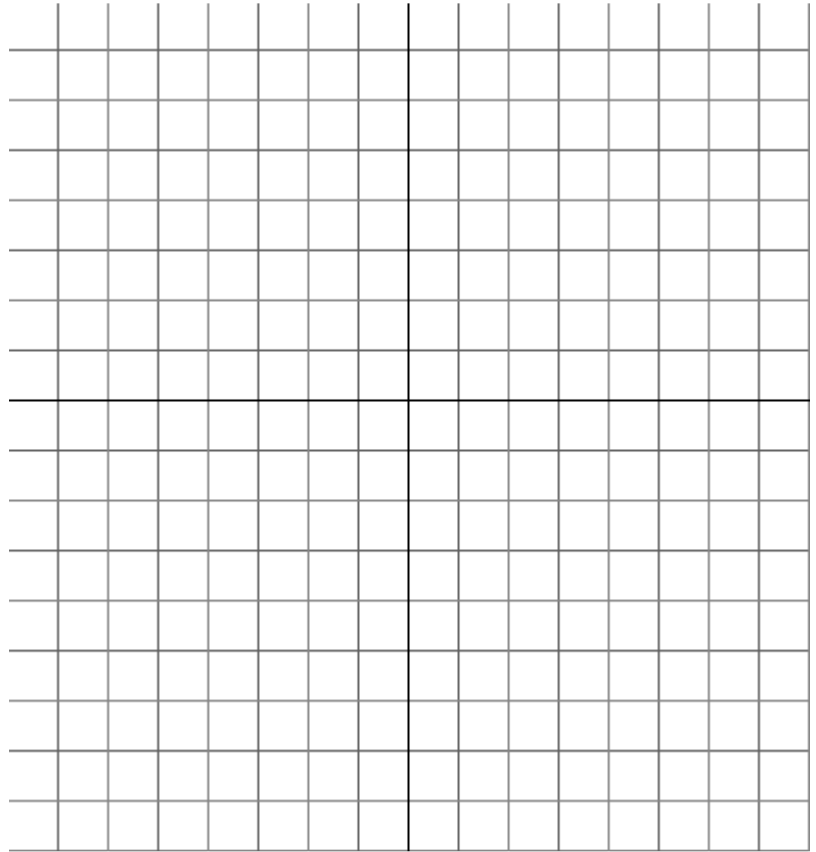
(a) The portion of the graph of $f(x) = 3x^{2/3} - 10$ from $(8,2)$ to $(27,17)$.

(b) The portion of the graph of $y = \frac{x^3}{12} + \frac{1}{x}$ from $x = 1$ to $x = 2$.

[4] Find the arc length of the graph of function over the indicated interval.

(a) $y = \ln(\cos x)$, $\left[0, \frac{\pi}{3}\right]$

- [5] Write a definite integral representing the volume of the solid generated by revolving the region bounded by the graphs of $y = \frac{10}{x^2}$, $y = 0$, $x = 1$, and $x = 5$ about the line $y = 10$.



[6] Evaluate each integral.

$$(a) \int \frac{6}{\sqrt{x}(1+x)} dx$$

$$(b) \int \frac{1}{\sqrt{e^{2x}-16}} dx$$

$$(c) \int_2^3 \frac{1}{\sqrt{4x-x^2}} dx$$

$$(d) \int \frac{1}{x\sqrt{x^6-1}} dx$$