

[1] Determine if each of the following *sequences* converges or diverges. If it converges, indicate the limit.

(a) $a_n = \frac{n}{\ln n}$

(b) $a_n = \frac{(-1)^n}{n^2 + 2n}$

(c) $a_n = (-1)^n \sqrt[n]{n}$

(d) $a_n = \frac{\sqrt{2n^2 + 1}}{3n + 2}$

[2] Find the sum of the following convergent series: $\sum_{n=1}^{\infty} \frac{(-1)^n 2^{n+1}}{5^n}$

[3] Determine if each series converges or diverges. Indicate the convergence tests used.

(a) $\sum_{n=1}^{\infty} \frac{2n+3}{\sqrt{5n^2+1}}$

(b) $\sum_{n=1}^{\infty} \frac{(2n)!}{n3^{n+1}}$

$$(c) \sum_{n=2}^{\infty} \frac{1}{n(\ln n)^{3/2}}$$

$$(d) \sum_{n=1}^{\infty} \frac{n + 3^n}{4^n}$$

[4] Determine if each series is *absolutely* convergent, *conditionally* convergent, or divergent. Indicate the convergence tests used.

$$(a) \sum_{n=1}^{\infty} (-1)^{n+1} \frac{(n+1)^n}{(2n+3)^n}$$

$$(b) \sum_{n=1}^{\infty} \frac{(-1)^n}{\sqrt{3n+1}}$$

$$(c) \sum_{n=1}^{\infty} (-1)^n \frac{n^2 + 3}{2n^4 + 3n + 1}$$

$$(d) \sum_{n=0}^{\infty} \frac{\cos^n n}{(n+2)^n}$$

[5] Determine the *radius* of convergence for each of the following power series.

$$(a) \sum_{n=0}^{\infty} \frac{2^n (x-1)^n}{n!}$$

$$(b) \sum_{n=1}^{\infty} n^n x^n$$

[6] Find the *interval* of convergence of the following power series.

$$(a) \sum_{n=1}^{\infty} \frac{1}{n} (x+1)^n$$

$$(b) \sum_{n=0}^{\infty} \frac{n!}{(2n)!} (x+1)^n$$

[7] Let $f(x) = \sum_{n=1}^{\infty} \frac{2^n}{n} (x-1)^n$. Find: (a) $f'(x)$, (b) $\int f(x) dx$, (c) the intervals of convergence for $f'(x)$, $f(x)$, and $\int f(x) dx$.