SI Session: June 23rd Mondays – Thursdays 12:30 PM – 2:00 PM Room 1229 Prof. Stockton : Calculus I Summer I 2008 SI Leader : Neil Jody

[1] Find the derivative of each function. DO NOT simplify your answer.

(a)
$$f(x) = \frac{\sin(\pi x)}{x+3}$$

(b)
$$f(x) = x^5 \sec\left(\frac{1}{x}\right)$$

(c)
$$f(x) = \frac{2x}{x^2 + 1}$$

(d)
$$f(x) = (\sqrt{x} + 3x) \left(5x^2 - \frac{3}{x} \right)$$

(e)
$$f(x) = \cos^3\left(\frac{x}{x+1}\right)$$

(f) $f(x) = \sin(x)\sec(x)$

(g)
$$f(x) = \frac{x^2 + \tan(x)}{3x + 2\tan(x)}$$

[2] Find the following derivatives using *implicit differentiation*.

(a)
$$\frac{d}{dx} \left[x^2 y + 3xy^3 - x = 3 \right]$$

(b)
$$\frac{d}{dx}\left[x^2 = \frac{x+y}{x-y}\right]$$

(c)
$$\frac{d}{dx} \left[\cos(xy^2) = y \right]$$

[3] A runner starts at a point "A" and heads East at a rate of 10 ft/sec. One minute later another runner starts at "A" heading North at 8 ft/sec. At what rate is the distance between them changing 1 minute after the 2nd runner starts?

[4] Boyle's law for gases states that pv=c, for pressure p, volume v, and a constant c. At a certain instant the volume in 75 *in*³, the pressure is $30 lb/in^2$, and the pressure is decreasing at a rate of $2 lb/in^2$ /min. At what rate is the volume changing at this instant?