SI Session: March, 24th & 26th, 2009 Tuesdays: 3:30 PM – 5:00 PM Thursdays: 1:30 PM – 3:00 PM & 3:30 PM – 5:00 PM Room 1245 SNAD

Prof. Stockton : Calculus I Spring 2009 SI Leader : Neil Jody

[1] For each of the following functions, find the open intervals on which the function is increasing or decreasing, and find the relative extrema.

(a)
$$f(x) = x^{\frac{2}{3}}(16 - x^2)$$

(b)
$$f(x) = \frac{x^2 - 9}{(x+1)^2}$$

(c)
$$f(x) = \frac{12x}{x^2 + 4}$$

[2] For each of the following functions, find the intervals on which the function is concave up or down, and identify any inflection points.

(a) $f(x) = -2x^4 + 8x^3$

(b)
$$g(x) = 3x^5 + 10x^4 - 7$$

(c)
$$h(x) = 3x^4 + 2x^3 - 12x^2 + 3x - 2$$

- [3] The graph of the *derivative* of a function f is given below. Use the graph to determine each of the following:
 - (a) the relative maxima of *f*(b) the relative minima of *f*



- [4] Sketch the graph of a function *f* that satisfies the following conditions:
 - f is increasing on $(-\infty, -2)$ and $(1, \infty)$; f is decreasing on (-2, 1)
 - *f* is concave down on $(-\infty, -1)$ and concave up on $(-1, \infty)$
 - the graph of *f* is everywhere smooth

Be sure to label any inflection points.



[5] Find the oblique asymptote for the following functions.

(a)
$$f(x) = \frac{x^2 - 6x + 12}{x - 4}$$

(b)
$$f(x) = \frac{x^3 - 4x^2}{x^2 - x - 12}$$

[6] As sand leaks out of a hole in a container, it forms a conical pile whose height is always equal to its radius. If the height of the pile is increasing at a rate of 6 in/min, find the rate at which the sand is leaking out when the height is 10 inches.