

Directions:

Take limits going to infinity. Take limits from both left and right at all points of discontinuity.

Find $\frac{d}{dx}$, 1st by definition, then by rules.

1.) $f(x) = \frac{\sin(\pi x)}{x + 3}$

2.) $f(x) = \frac{\cos\left(\frac{\pi}{x}\right)}{x - 2}$

3.) $f(x) = \frac{\sin(2x) - 2\sqrt{x} \sin x + 4x^2}{x}$

4.) $f(x) = \frac{\sqrt{3x^4 + x}}{x^2 - 8}$

5.) $f(x) = \sqrt[3]{\frac{2 + 3x - 5x^2}{1 + 8x^2}}$

6.) $f(x) = \frac{\cos^2(x)}{x}$

7.) $f(x) = \frac{\sqrt{4x^2 + 5x}}{x - 1}$

8.) $f(x) = \frac{2 - x}{\sqrt{7 + 6x^2}}$

9.) $f(x) = \frac{|x^2 - 4|x}{x + 2}$

Tips: $\frac{\text{Big \#}}{\text{Small \#}} = \text{Huge \#} \Rightarrow \pm \infty$;

$\frac{\text{Small \#}}{\text{Big \#}} = \text{tiny \#} \Rightarrow 0$

10.) $f(x) = \frac{4x - 3}{\sqrt{x^2 + 1}}$

11.) $f(x) = \frac{\sqrt{x} - \sqrt{2}}{x - 2}$

12.) $f(x) = \frac{x^4 - 16}{x^2 - x - 2}$

13.) $f(x) = \frac{\sqrt{4 - 9x^2}}{x^2}$

Derivatives:

1.) $f(x) = \frac{1}{\sqrt{x - 1}}$

2.) $f(x) = \sqrt{\frac{x}{2}}$

3.) $f(x) = 3 + \frac{2}{x - 1}$

Practice: Simplify into Lowest Terms

$$\frac{1}{h} \left[\frac{2(x+h)+3}{(x+h)-1} - \frac{2x+3}{x-1} \right]$$

$$\frac{A}{2\sqrt{Ax - B^2}} - \left[\frac{B}{1 + \frac{Ax - B^2}{B^2}} \cdot \frac{A}{2B\sqrt{Ax - B^2}} \right]$$