

Directions: Evaluate and/or calculate as indicated.

1. A window has the shape of a rectangle surmounted by a semicircle. If the perimeter of the window is 15 ft, find the dimensions that will allow the maximum amount of light to enter.

$$2. \int \frac{x^3 - x + 2}{\sqrt{x}} dx$$

$$3. \int_3^6 x^2 \sqrt{x-2} dx$$

$$4. \int \frac{\sin(\sqrt{x} + 3)}{\sqrt{x}} dx$$

$$5. \int \frac{3 \cos(4 + \frac{1}{x})}{x^2} dx$$

$$6. \int_0^{\pi/3} \sin x \cos^2 x dx$$

$$7. \int_1^e \frac{(\ln x)^4}{x} dx$$

$$8. \int_4^9 \frac{1}{\sqrt{x}(2\sqrt{x}-3)} dx$$

$$9. \int \frac{3x}{4+x^2} dx$$

$$10. \int \frac{\sin(\ln x)}{x} dx$$

$$11. \int_0^{\pi/6} \frac{\cos x}{2\sin x + 1} dx$$

$$12. \int \frac{\tan \sqrt{x}}{\sqrt{x}} dx$$

$$\text{Tips: } \int cf(x) dx = c \int f(x) dx,$$

$$\int [f(x) \pm g(x)] dx = \int f(x) dx \pm \int g(x) dx$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \text{ if } n \neq -1$$

$$13. \int \frac{2x^2 - x + 3}{\sqrt{x}} dx$$

$$14. \int (\cos x + \sin x)^2 dx$$

$$15. \int \frac{3x + 6}{\sqrt[3]{x^2 + 4x - 3}} dx$$

$$16. \int \frac{x}{(4-x)^3} dx$$

$$17. \int_0^{\pi/2} \sin x \sqrt{3 \cos x + 1} dx$$

$$18. \int \sec^2\left(\frac{x}{3}\right) \tan^2\left(\frac{x}{3}\right) dx$$

$$19. \int_{-2}^3 |2x - 4| dx$$

Find $\frac{dy}{dx}$ for the following.

$$20. y = \ln\left(\frac{x^2 \sin x \sqrt{2x+3}}{(x^2+4) \ln x}\right)$$

$$21. y = \tan(\ln \sqrt{x})$$

$$22. y = \ln(\sin(3x))$$

$$23. \ln(xy^2) = \cos x$$